

# Basic Mathematics



Marcella L. Morgan R.N., M.S.N.

# Roman Numerals



- $ss = \frac{1}{2}$
- **I** = 1 or i
- II = 2 or ii
- III = 3 or iii
- IV = 4 or iv
- **V** = 5
- VI = 6
- VII = 7
- VIII = 8
- IX = 9
- **X** = 10
- XI = 11 or xi
- XII = 12 or xii
- XIV = 14
- XV = 15
- XIX = 19
- XX = 20
- XXXIX = 39
- **XL** = 40
- **LI** = 51
- **LX** = 60

# Fractions

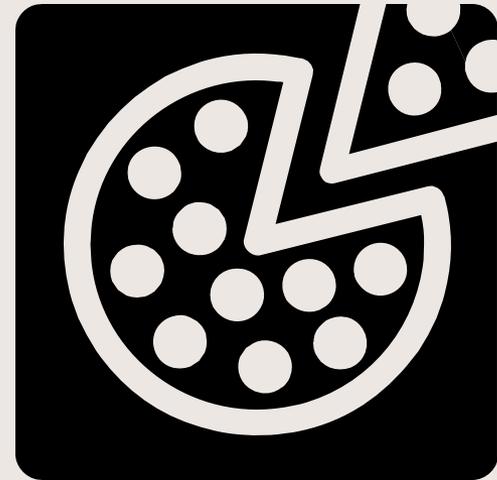


- Part of whole number

$$\frac{6}{8}, \frac{6}{8} \text{ (numerator)}$$
$$\frac{6}{8} \text{ (denominator)}$$

Can be reduced by division

$$\frac{3}{4}, \frac{3}{4}$$



# Types of Fractions

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- Proper Fractions:  $\frac{3}{4}$
- Mixed numbers:  $2 \frac{1}{3} = 2 + \frac{1}{3}$
- Improper fractions:  $\frac{3}{3}$  or  $\frac{8}{3}$

# Proper Fractions

- Always reduce proper fractions to its lowest form
- $8/10 = 4/5$
- $3/9 = 1/3$
- $8/16 = 1/2$
- $3/12 = 1/4$

# Mixed Numbers

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- $5 \frac{4}{8} = 5 \frac{1}{2}$
- $16 \frac{4}{6} = 16 \frac{2}{3}$
- $7 \frac{3}{9} = 7 \frac{1}{3}$
- $11 \frac{12}{16} = 11 \frac{3}{4}$

# Improper Fractions

- Numerator larger than denominator ie:  $8/4$  or  $16/6$
- $8$  divided by  $4 = 2$  (Whole number)
- $16$  divided by  $6 = 2 \frac{4}{6}$  (Mixed Number)
- $2 \frac{4}{6} = 2 \frac{1}{3}$

# Changing Mixed Numbers to Improper Fractions

$$2 \frac{3}{8} = 8 \times 2 + 3 = \underline{19} \text{ (numerator)}$$
$$8 \text{ (denominator)}$$

$$4 \frac{2}{5} = 5 \times 4 + 2 = \underline{22} \text{ (numerator)}$$
$$5 \text{ (denominator)}$$

# Adding & Subtracting Fractions

- Denominators **MUST** be the same
- Add or subtract numerators
- $5/16 - 2/16 = 3/16$
- $3/8 + 1/8 = 4/8$  or  $1/2$
- $3/4 + 1/4 = 4/4$  or  $1$

# Common Denominator

- Number that can be divided evenly by **ALL** the denominators in the problem
- $5/16 - 1/8$
- $3/8 + 2/16$
- $3/4 = 2/8$

# Changing a Fraction

- Whatever is done to the denominator (multiply or division) must be done to the numerator
- $5/16 - 1/8 = 5/16 - 2/16$

# Addition of Fractions and Mixed Numbers

- $1/5 + 2/5 = 3/5$
- $2/6 + 1/6 = 3/6$  reduced to  $1/2$
- $7/10 + 8/15 = 21/30 + 16/30 = 36/30$
- $36/30 = 6/5$  (improper fraction)
- $6/5 = 1 \frac{1}{5}$  (mixed number)

# Adding & Subtracting Mixed Numbers

- $9 \frac{5}{8} + 6 \frac{1}{6}$

- 1<sup>st</sup> step:  $\frac{5}{8} + \frac{1}{6}$

$$\frac{15}{24} + \frac{4}{24} = \frac{19}{24}$$

- $9 + 6 = 15$

- Answer:  $15 \frac{19}{24}$

# Value of Fractions

$\frac{1}{7}$						
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$\frac{1}{9}$								
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$\frac{1}{5}$	$\frac{1}{5}$	$\frac{1}{5}$	$\frac{1}{5}$	$\frac{1}{5}$
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# Which is Greater ?

$\frac{1}{3}$  or  $\frac{1}{5}$

$\frac{1}{250}$  or  $\frac{1}{300}$

$\frac{1}{10}$  or  $\frac{1}{7}$

$\frac{1}{4}$  or  $\frac{2}{8}$



# Which is Less ?

- $1/100$  or  $1/125$
- $1/7$  or  $1/9$
- $1/50$  or  $1/100$
- $3/4$  or  $2/8$



# Review

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- Roman Numerals
- 3 types of fractions
- Reduction of fractions
- Addition & subtraction of fractions & mixed numbers
- Value of fractions

# Multiplying Fractions

- Change the mixed number to an improper fraction

- $4 \frac{1}{2} \times 2 \frac{1}{4}$

- $(2 \times 4) + 1 \times (4 \times 2) + 1 = (8) + 1 \times (8) + 1$

- $\frac{9}{2} \times \frac{9}{4}$

- Multiply numerators

- $9 \times 9 = 81$

- Multiply denominators

- $2 \times 4 = 8$

- $\frac{81}{8}$

- Reduce

- $10 \frac{1}{8}$

# Division of Fractions

- Change mixed numbers to improper fractions
- Invert the number after the division sign and multiply
- $1/2$  divided by  $5/8$
- $1/2 \times 8/5 = 8/10$
- $4/5$

# Decimals

- Fraction whose denominator is 10, 100, 1000, or 10,000
- All whole numbers are to the left of the decimal point
- Decimal fractions are to the right
- $0.257 = 257/1000$
- $0.2057 = 2057/10,000$
- $327.006 = 327 \frac{6}{1000}$

# Comparison of Decimals

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- 0.4 or 0.2
- 0.68 or 0.8
- 1.465 or 1.29
- 5.12 or 0.512
- 0.005 or 0.015
- 0.25 or 0.250
- .826 or .830

# Addition & Subtraction of Decimals

- Keep all decimals in column with decimal points lined up
- Place decimal point directly under the decimal points in the problem

$$\begin{array}{r} 0.8 \\ + 0.5 \\ \hline 1.3 \end{array} \quad \begin{array}{r} 3.27 \\ + 0.06 \\ \hline 3.33 \end{array} \quad \begin{array}{r} 4.50 \\ - 0.75 \\ \hline 3.75 \end{array} \quad \begin{array}{r} 0.45 \\ - 0.09 \\ \hline 0.36 \end{array}$$

# Multiplication of Decimals

- $2.6 \times 0.0002$

- $$\begin{array}{r} 2.6 \quad (\text{one decimal point}) \\ \times 0.0002 \quad (\text{four decimal point}) \\ \hline \end{array}$$

**0.00052** (5 decimal point)

# Division of Decimals

- Is the divisor a whole number or a decimal?
- Make the divisor a whole number
- Divide as whole number
- Refer to pages 20 & 21 in text

# Changing Decimals to Fractions and Vise Versa

- 0.375
- 375/1000
- 0.91
- 91/100
- 0.4
- 4/10

**EASY RULE:** To change **decimals to fractions**, the amount of numbers on top (the numerator) will equal the amount of zeros on the bottom (the denominator)

To change **fractions to decimals**, it is just the opposite. The amount of zeros on the bottom will equal the amount of “places” after the decimal

# Rounding Decimals

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- $2.7 = 3$  (rounding to whole number)
- $2.55 = 2.6$  (rounding to tenths)
- $3.762 = 3.76$  (rounding to hundredths)

# Percentages, Decimals & Fractions

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- Percent (%) means *per hundred*
- 25% means 25 *per hundred*

$$25\% = 25/100 = .25$$

$$50\% = 50/100 = .50$$

# Finding the Percentage

- Change the % to a decimal or common fraction
- Multiply the number by this decimal
- $23\%$  of  $64 = 64 \times 0.23 = 14.72$
- $5\%$  of  $10 = 10 \times 0.05 = 0.5$

# Ratios & Proportions

Ratio is the relationship of one quantity to another

$$1/3 = 1 : 3$$

$$1/2 = 1 : 2$$

Give 1 mg for each kg of body weight.

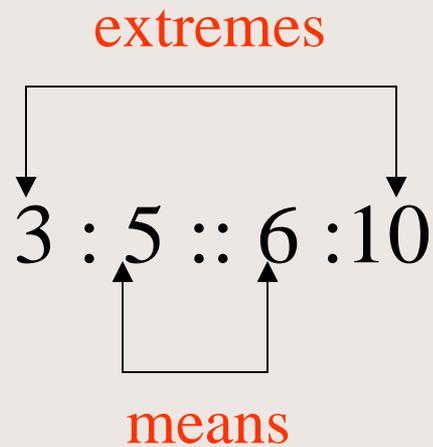
$$1\text{mg}/1\text{kg} \text{ or } 1\text{mg} : 1\text{kg}$$

# Ratios as Fractions

- $3:6 = \frac{3}{6}$  or  $\frac{1}{2}$
- $5:7 = \frac{5}{7}$
- $4:20 = \frac{4}{20}$  or  $\frac{1}{5}$
- $5:30 = \frac{5}{30}$  or  $\frac{1}{6}$
- $7:49 = \frac{7}{49}$  or  $\frac{1}{7}$
- $2:38 = \frac{2}{38}$  or  $\frac{1}{19}$
- $6:85 = \frac{6}{85}$
- $9:81 = \frac{9}{81}$  or  $\frac{1}{9}$

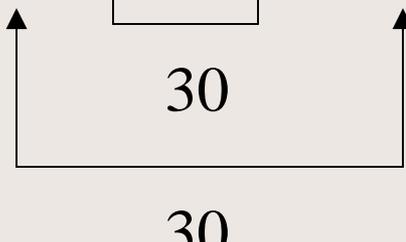
# Proportions

- Relationship between two equal ratios.
- Expressed as  $3 : 5 :: 6 : 10$   
 $3 : 5 = 6 : 10$



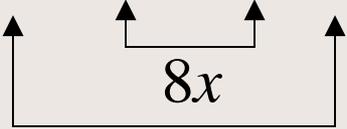
# Solving Ratio/Proportion Problems

- Multiply the **EXTREMES**
- Multiply the **MEANS**
- Answers should be the same

- $3 : 5 :: 6 : 10$   


- $\begin{matrix} (e) & \frac{3}{5} & \begin{matrix} \nearrow & \nwarrow \\ \nwarrow & \nearrow \end{matrix} & \frac{6}{10} & (m) \\ (m) & & & & (e) \end{matrix}$   
 $3 \times 10 = 30$   
 $5 \times 6 = 30$

$$2 : 8 :: x : 24$$

- $2 : 8 :: x : 24$   
  
48

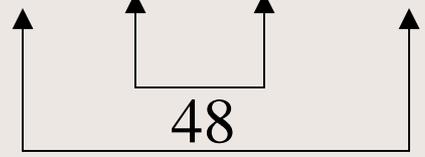
- $8x = 48$

- $\frac{8x}{8} = \frac{48}{8}$

- $x = 6$

Check your answer

$$2 : 8 :: 6 : 24$$

$$2 : 8 :: 6 : 24$$
  
  
48

# Setting Up Ratios & Proportions

- Always put on the left hand side of the (=) what you already have or know
- The  $X$  goes on the right hand side. This is what you want to know.  $6 : 4 :: x : 30$
- Each side of the equation is set up the same way
- After multiplying, place  $x$  on the left side of the (=) sign to solve.  $4x = 180$
- $X = 45$

# Setting Up Ratios & Proportions

- Know                      6 bananas : 9 apples
- Want to know             $x$  bananas : 72 apples
  
- $6 : 9 :: x : 72$
- $9x = 432$
- $x = 48$
- $6 : 9 :: 48 : 72 \longrightarrow 432 = 432$

# Setting Up Ratios & Proportions

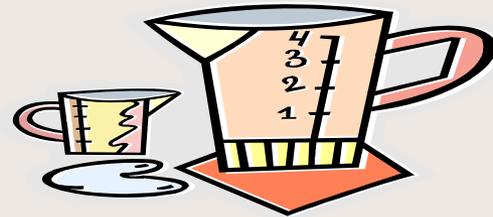
- The order is for 100 mg. The pharmacy sends 50 mg tablets. How many tablets will the nurse give?
- 50 mg : 1 tablet
- 100 mg :  $x$  tablets
- 50 mg : 1 tablet : 100 mg :  $x$  tablets
- Solve for  $x$
- $X = 2$  tablets

# Systems of Measurement

- Metric System



- Household System



- Apothecary Apothecary



# Metric System



# Metric System

- **Weight:** Gram
- **Volume:** Liter
- **Length:** Meter



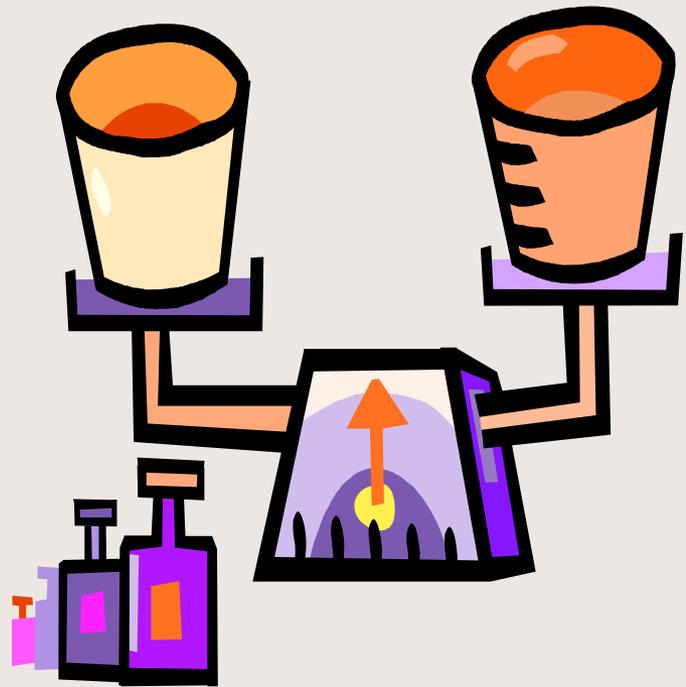
# Metric System

$$\text{Micro} = \frac{1}{1,000,000}$$

$$\text{Centi} = \frac{1}{100}$$

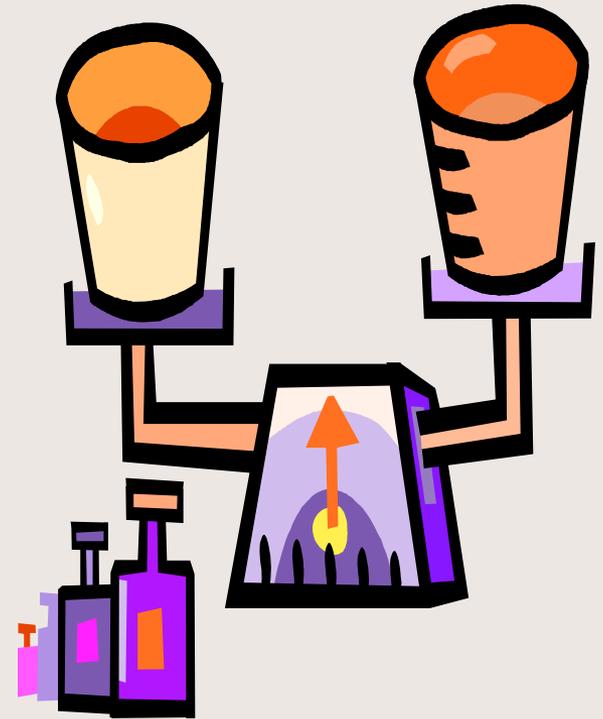
$$\text{Milli} = \frac{1}{1,000}$$

$$\text{Kilo} = 1,000$$



# Metric System

- Milli + liter = milliliter  
0.001 of a liter
- Micro + gram = microgram  
0.000001 of a gram
- Kilo + meter = kilometer  
1,000 meters





# Metric System



## WEIGHT

- Gram Gm
- Microgram mcg
- Milligram mg
- Kilogram Kg

## VOLUME

- Liter L
- Milliliter ml
- Cubic Centimeter cc

# Metric Conversions

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- 1000 mg = kg
- 0.75 L = ml
- 450 mm = cm
- 10,000 mcg = grams
- 1kg = mg

# Metric Conversions

Kilo	Hecto	Deka	<u><i>UNIT</i></u>	Deci	Centi	Milli
1,000	100	10		1/10	1/100	1/1000

$$1000 \text{ mg} = \text{g}$$

$$160 \text{ cm} = \text{mm}$$

$$10 \text{ L} = \text{ml}$$

$$109 \text{ g} = \text{kg}$$

# Metric Conversion

Kilo 1,000	Hecto 100	Deka 10	<u><i>UNIT</i></u>	Deci 1/10	Centi 1/100	Milli 1/1000
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**K**  
I  
N  
G

**H**  
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R  
Y

**D**  
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# Rounding Medication Doses

**Remember**: Seldom should a patient receive more than one or two multiples of the unit dose supplied.

Rx: 750mg

Have: 300mg tabs

Call Pharmacy



# Rounding Medications

- **RULE:** Always round your answers to the nearest measurable dose **AFTER** verifying the dose is correct for that patient
- If tablets are scored, you may break.
- Never break unscored tablets.
- Recheck if dose is  $> 2$  tablets.

# Rounding Milliliters (ml or cc)

- **RULE:** To round to the nearest tenth, examine the hundredths column. If it's 0.05 or greater, round up to the next tenth. If it is 0.04 or less, the tenths column remains the same.

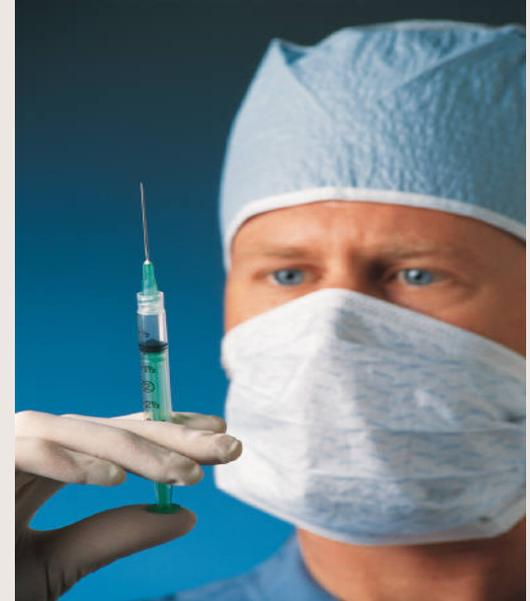
- 1.75ml → 1.8ml

- 1.53ml → 1.5ml



# Rounding Milliliters

- **RULE:** To round to the nearest hundredth, examine the thousandths column. If 0.005 or greater, round up to the next hundredth.
- 0.756ml round to 0.76ml
- 0.754ml round to 0.75ml



# CLINICAL ALERT

- Never round up liquid medications to the nearest whole number.
- 1.7ml does not round up to 2ml
- Use a medication cup, spoon, dropper or needles syringe



# Metric System Rules

- 1. ARABIC numbers are used to express quantities
- 2. Parts of a unit are expressed as DECIMALS. Fractions are never used
- 3. The quantity is ALWAYS written before the abbreviation or symbol of the unit of measure